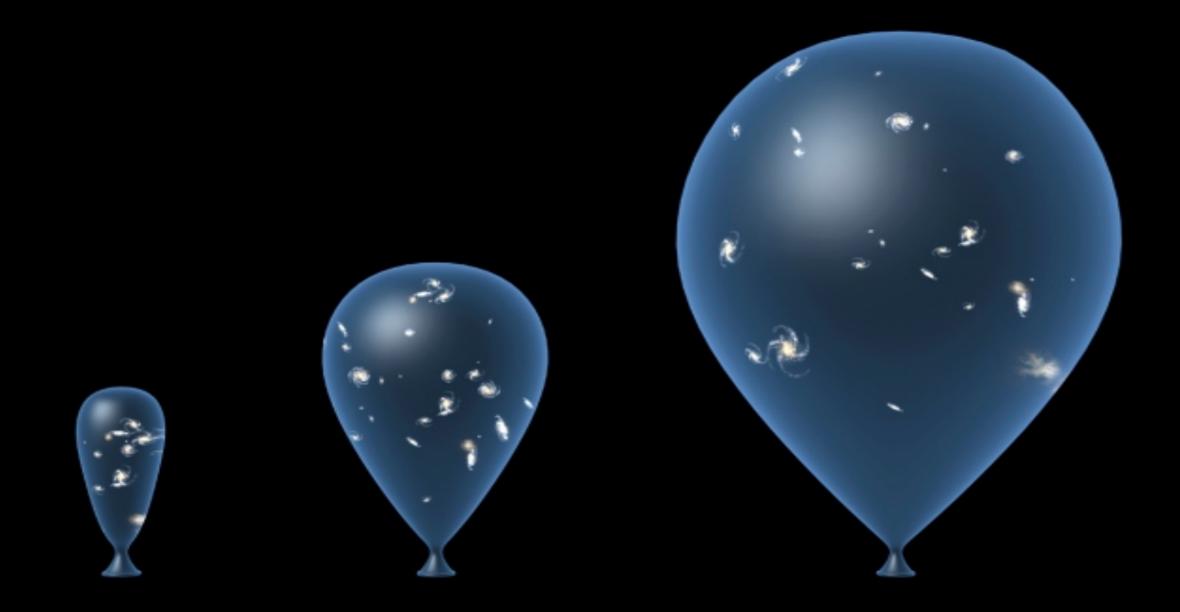


The Big-Bang theory

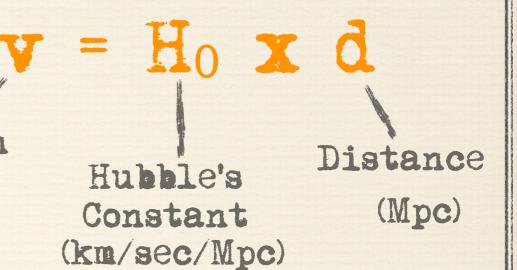
Luis Anchordoqui

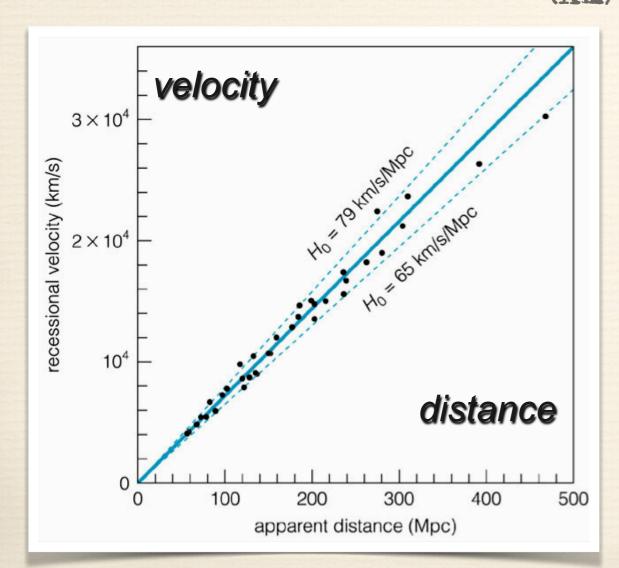
Last class....



Hubble's Law

Velocity of Recession (Doplpler Shift) (km/sec)





Implies the Expansion of the Universe

The redshift of a Galaxy is:

- A. The rate at which a Galaxy is expanding in size
- B. How much reader the galaxy appears when observed at large distances
- C. The speed at which a galaxy is orbiting around the Milky Way
- D. The relative speed of the redder stars in the galaxy with respect to the blues stars
- E. The recessional velocity of a galaxy, expressed as a fraction of the speed of light

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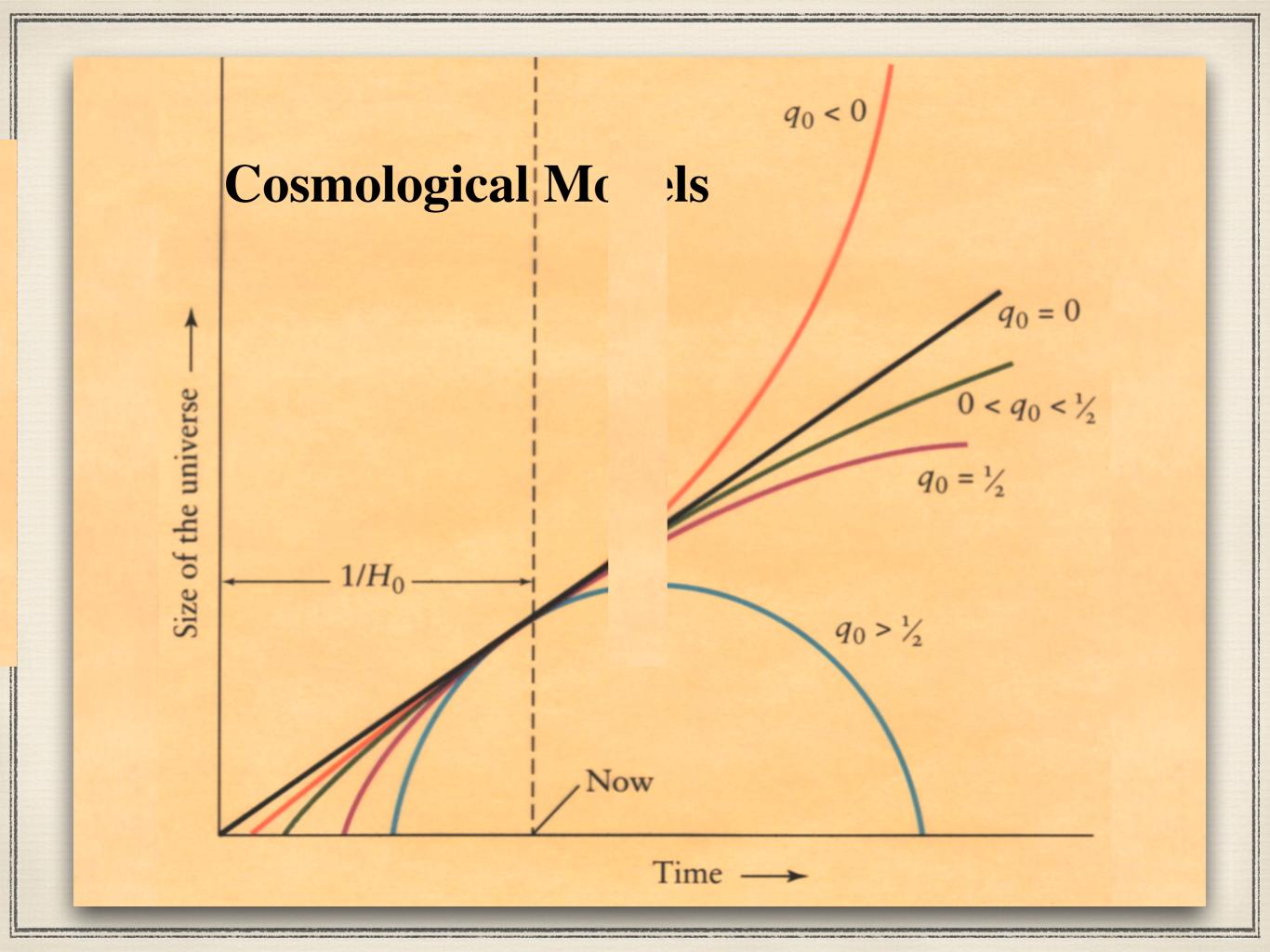
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To a first approximation, a rough maximum age of the Universe can be estimated using which of the following?

- A. The age of the oldest open clusters
- B. 1/H₀ the Hubble time
- C. The age of the Sun
- D. The age of the Galaxy
- E. There is no simple estimate

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- D. The age of the Galaxy
- E. There is no simple estimate



The Early Cosmological Models

their names

Einstein in 1917 constructed the first relativistic cosmological models. Thinking that the universe is static, he introduced the cosmological constant term to balance the force of gravity. This model was unstable.

Willem De Sitter in 1917 also developed a similar model, but also obtained sclutions of Einstein equations for early empty expanding universe
In 1932, Einstein & De Sitter jointly developed another, simple cosmological model which bears

The Friedmann and Laitre Models

nder Friedmann

developed the GR-based, expanding se model. It was not taken very ly at the time, since the expansion

stablished

universe has not

Georges]

In 1927 independently developed cos models like Friedmanns. In 1933, he film backwards to a hot, dense, ea of the universe he called the co.

This early prediction of the Big Bang was

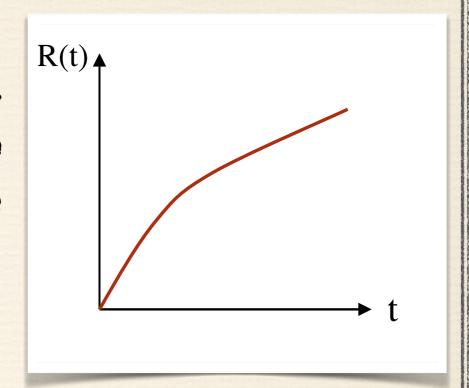
largely ignored.

They used the homogeneity and isotropy to reduce the full set of 16 Einstein equations of GR to one: the Friedmann-Lemaitre eqn.

Kinematics of the Universe

We introduce a scale factor, commonly denoted as R(t) or a(t): a spatial distance between any two unaccelerated frames which move with their comoving coordinates

This fully describes the evolution of a homogeneous, isotropic universe



Computing R(t) and various derived quantities defines the cosmological models. This is accomplished by solving the Friedmann (or Friedmann-Lemaitre) Equation

The equation is parametrized (and thus the models defined) by a set of cosmological parameters

Cosmological Parameters

Cosmological models are typically defined through several handy key parameters:

1. The Hubble Parameter

The Hubble parameter is the normalized rate of expansion

$$H = \frac{1}{R} \frac{\Delta R}{\Delta t}$$

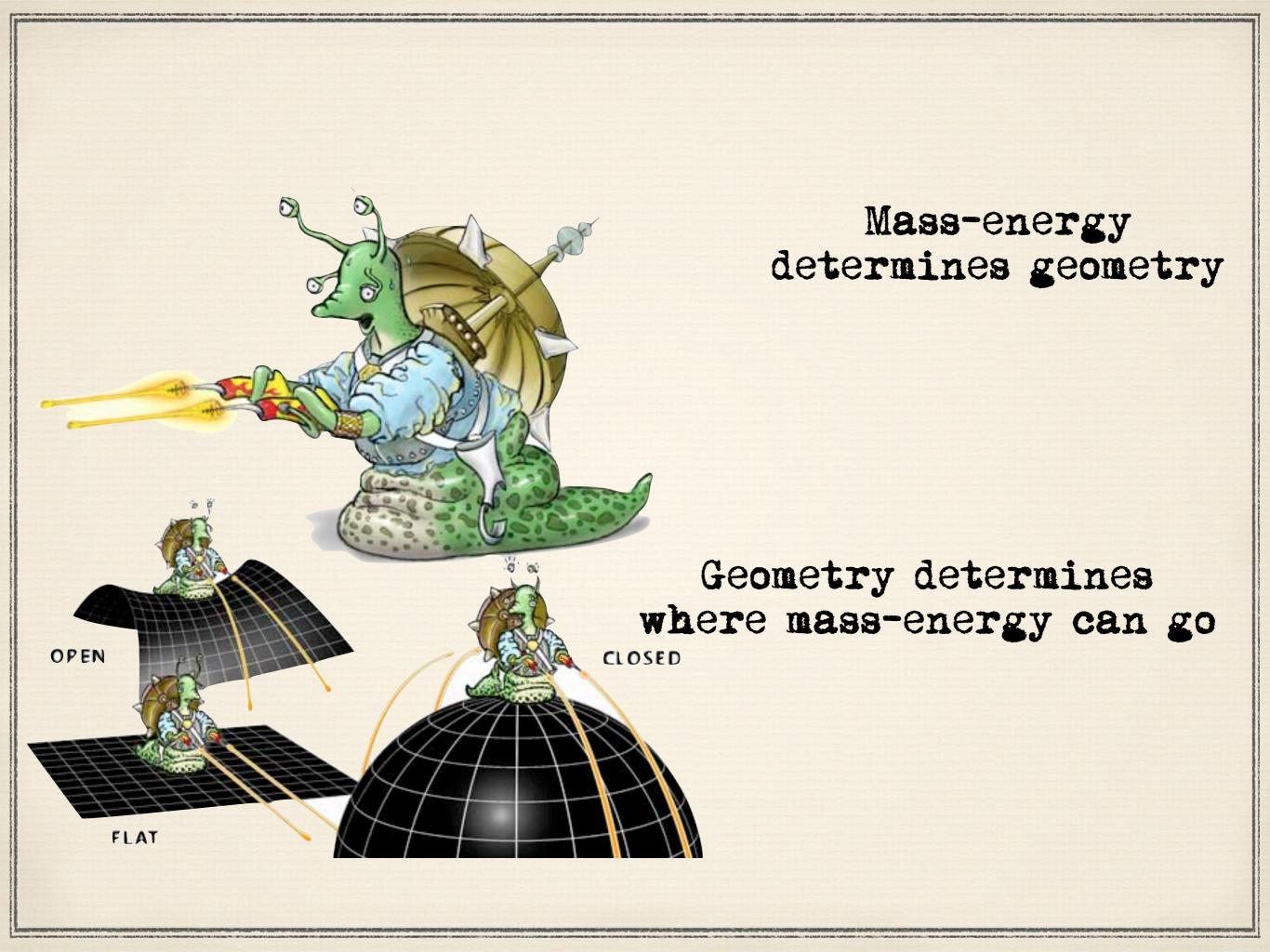
$$\Delta R = R_{final} - R_{initial}$$

$$\Delta t = t_{final} - t_{initial}$$

Note that the Hubble parameter is not a constant!

The Hubble constant is the Hubble parameter measured today - we denote its value by H_0

Current estimates are in the range of Ho = 65 - 75 km/s/Mpc



Cosmological Parameters

3. The matter Density parameter

Rewriting the Friedmann Eqn. Using the Hublle parameter and $\hat{\Lambda}$ or now set $\Lambda = 0$

$$I\Lambda^2 - \frac{8}{3}\pi G\rho = -\frac{kc^2}{R}$$

The Universe is flat if k = 0, or if it has a critical density of

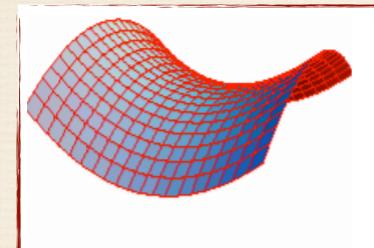
$$\rho_{crit} = \frac{3H^2}{8\pi G}$$

We define the matter density parameter as

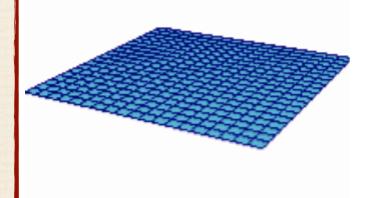
$$\Omega_M = \frac{\rho}{\rho_{crit}}$$

Geometry and the Fate of the Universe

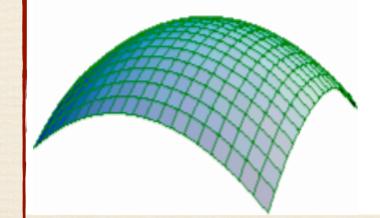
Matter and energy content of the universe determines its geometry (curvature of space), and the ultimate fate



 $\rho < \rho_{crit}, k = -1$ negative curvature expands for ever

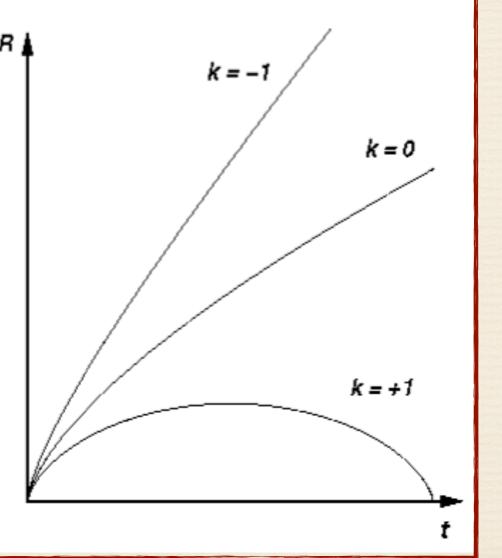


 $\rho = \rho_{crit}, k = 0$ flat (Euclidean)
expands for ever

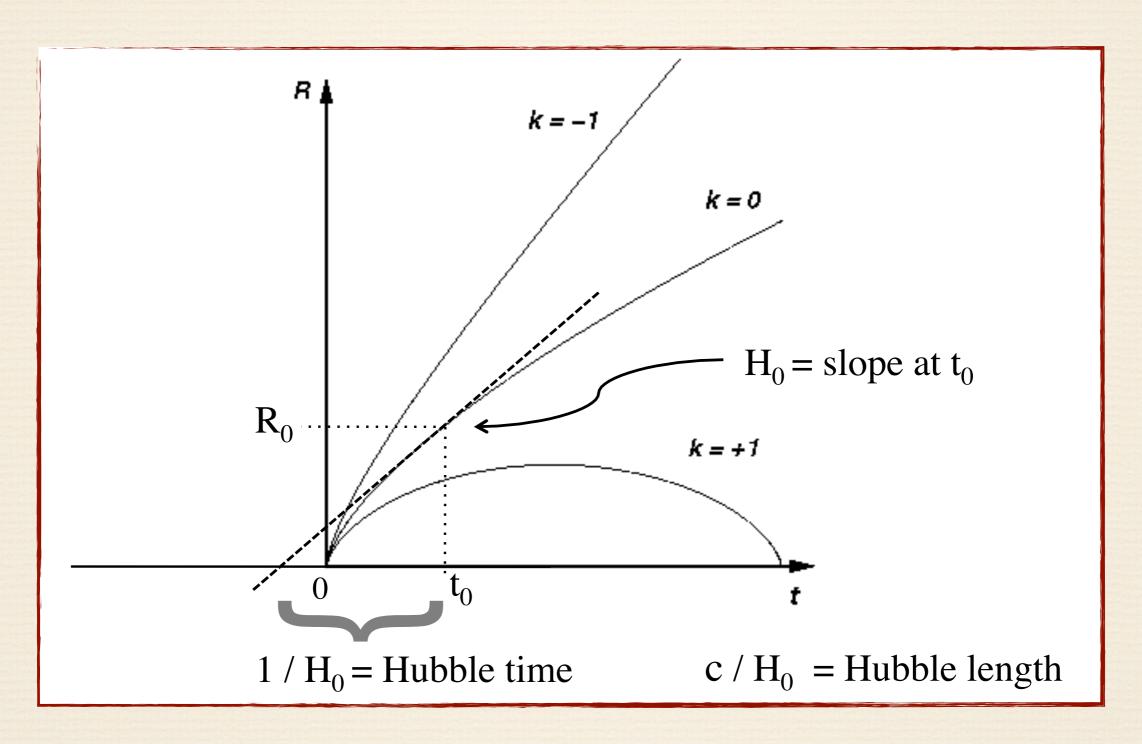


 $\rho > \rho_{crit}, k = +1$ positive curvature
collapses

Possible expansion histories:



Hubble Constant Defines the Scale of the Universe



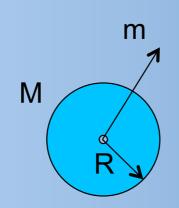
Critical Mass Density for the Universe

We can get an estimate of how much mass is needed to "close" the universe. More accurately, we calculate the mean density needed to close the universe.

We balance gravitational potential energy and kinetic energy using simple Newtonian mechanics.

E = 0 corresponds to mass m having escape velocity from M

Example: Earth $R \sim 6371 \text{ km}$ $M = 5.97 \times 10^{24} \text{ kg}$



Potential energy of mass m in gravitational field of M

$$PE = -\frac{GMm}{R}$$

Kinetic energy of mass m

$${\rm KE} = \frac{1}{2} m V^2$$
 Total energy:
$$E = {\rm KE} + {\rm PE} = \frac{1}{2} m V^2 - \frac{GMm}{R}$$

G = Gravitational constant

 $G = 6.67 \times 10^{-8} \text{ cm}^3 \text{ g}^{-1} \text{s}^{-2} \text{ or } G = 6.67 \times 10^{-11} \text{ m}^3 \text{ kg}^{-1} \text{ s}^{-2}$

$$V_{\rm esc} = \left(\frac{2GM}{R}\right)^{1/2}$$

$$V_{\rm esc} \sim 11.2 \text{ km/s}$$

Critical Mass Density for the Universe II

We can get an estimate of how much mass is needed to "close" the universe. More accurately, we calculate the mean density needed to close the universe.

We balance gravitational potential energy and kinetic energy using simple Newtonian mechanics.

E = 0 corresponds to mass m having escape velocity from M

Volume of sphere = $(4\pi/3)R^3$

This gives a mass density ρ_c (g / volume)

We can also solve for E = 0 from

$$E={\rm KE}+{\rm PE}=\frac{1}{2}mV^2-\frac{GMm}{R}$$
 to get
$$\frac{M}{R}=\frac{V^2}{2G}$$

Now we consider m to be any object in the universe and we relate its velocity to the Hubble law, $V = H_0R$

Then:
$$\frac{M}{R} = \frac{V^2}{2G} = \frac{(H_0 R)^2}{2G}$$

Or:
$$\frac{M}{R^3} = \frac{H_0^2}{2G}$$

$$\rightarrow \frac{M}{(4\pi/3)R^3} = \frac{H_0^2}{2G(4\pi/3)} = \frac{3H_0^2}{8\pi G}$$

$$\rho_c = \frac{3H_0^2}{8\pi G}$$

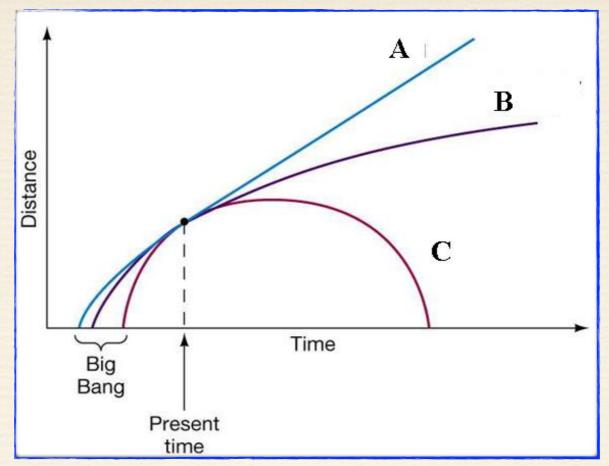
Critical mass density ~ 10⁻²⁹ g cm⁻³

If the density of the Universe is less than critical, then the Universe:

- A. Will ultimately collapse back in on itself
- B. Will expand forever
- C. Must be spherical
- D. Will have a temperature of 2.73K forever
- E. Must be static, with an unknown cause for the redshifts

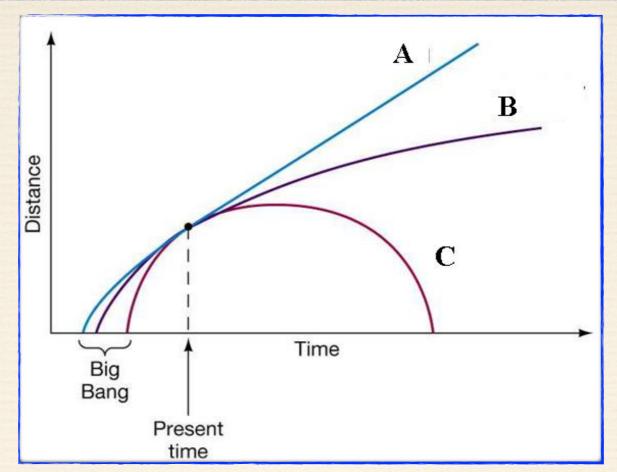
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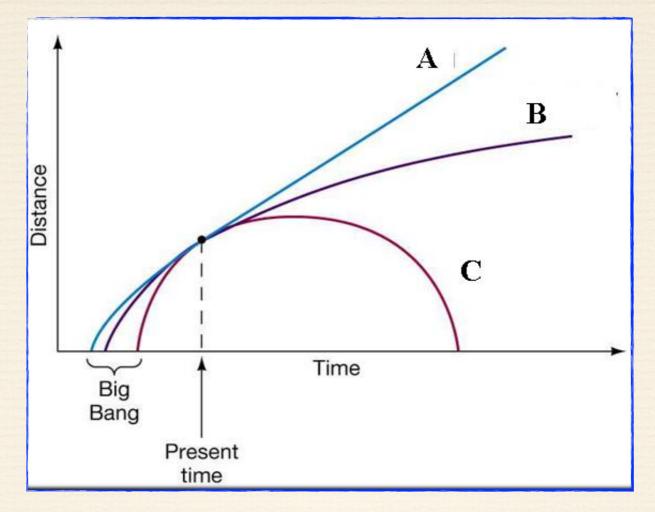
Curve A describes which type of Universe:

- A. Open, where the Universe will continue to expand forever
- B. Hyperbolic, where the expansion of the Universe becomes exaggerated
- C. Flat, where parallel lines never meet
- D. Closed, where the Universe will ultimately re-collapse
- E. Parallel, where multiple Universes parallel our own evolution



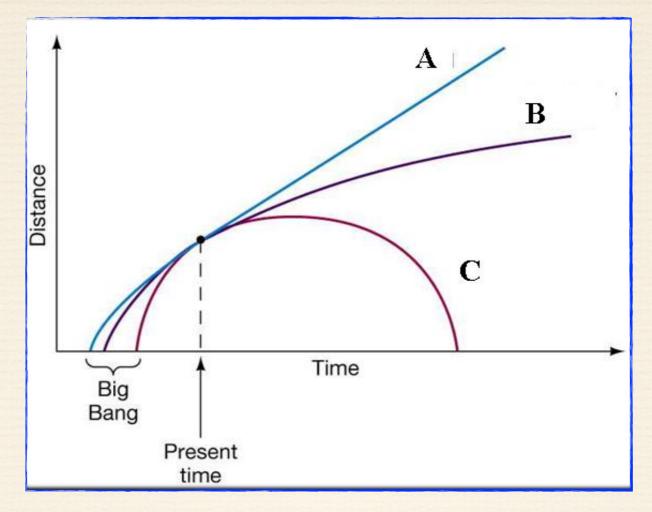
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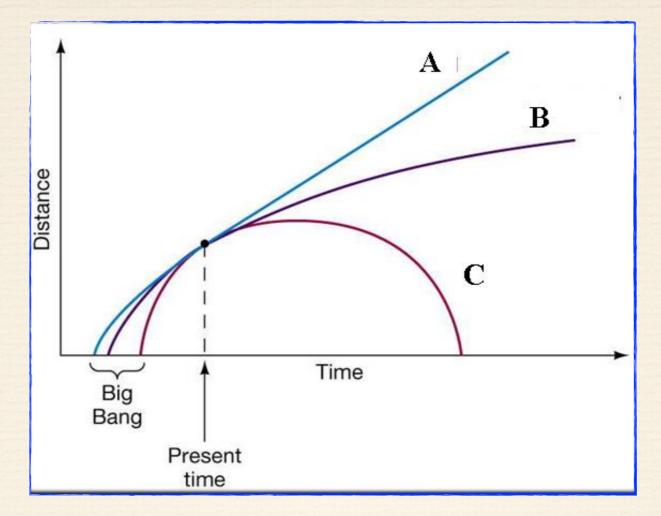
Curve B describes which type of Universe:

- A. Open, where the Universe will continue to expand forever
- B. Flat, where parallel lines never meet
- C. Parallel, where multiple Universes parallel our own evolution
- D. Hyperbolic, where the expansion of the Universe becomes exaggerated
- E. Closed, where the Universe will ultimately re-collapse



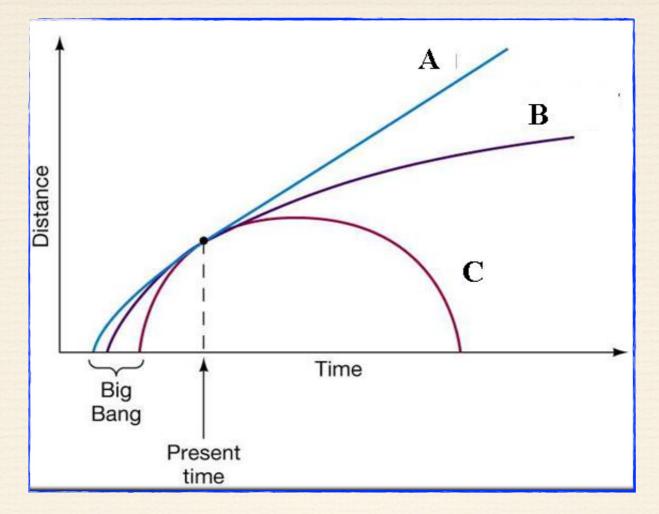
Curve B describes which type of Universe:

- A. Open, where the Universe will continue to expand forever
- B. Flat, where parallel lines never meet
- C. Parallel, where multiple Universes parallel our own evolution
- D. Hyperbolic, where the expansion of the Universe becomes exaggerated
- E. Closed, where the Universe will ultimately re-collapse



Curve C describes which type of Universe:

- A. Flat, where parallel lines never meet
- B. Parallel, where multiple Universes parallel our own evolution
- C. Closed, where the Universe will ultimately re-collapse
- D. Hyperbolic, where the expansion of the Universe becomes exaggerated
- E. Open, where the Universe will continue to expand forever



Curve C describes which type of Universe:

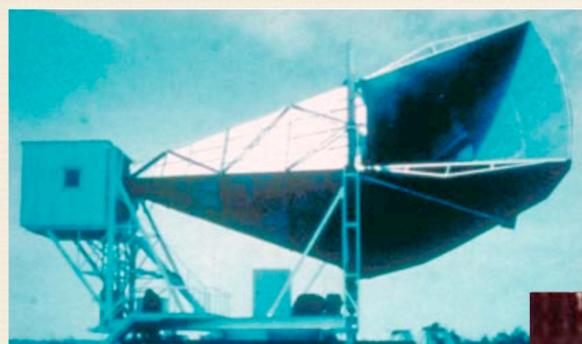
- A. Flat, where parallel lines never meet
- B. Parallel, where multiple Universes parallel our own evolution
- C. Closed, where the Universe will ultimately re-collapse
- D. Hyperbolic, where the expansion of the Universe becomes exaggerated
- E. Open, where the Universe will continue to expand forever

The Early Universe



and the Cosmic Microwave Background

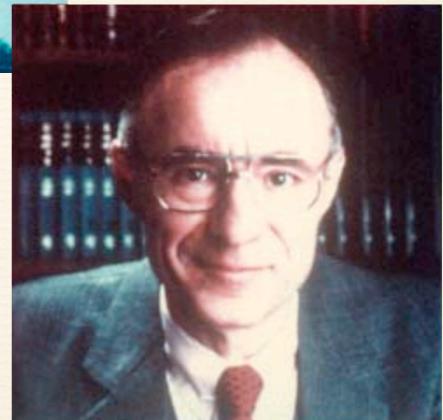
Discovery of cosmic background



Microwave Receiver

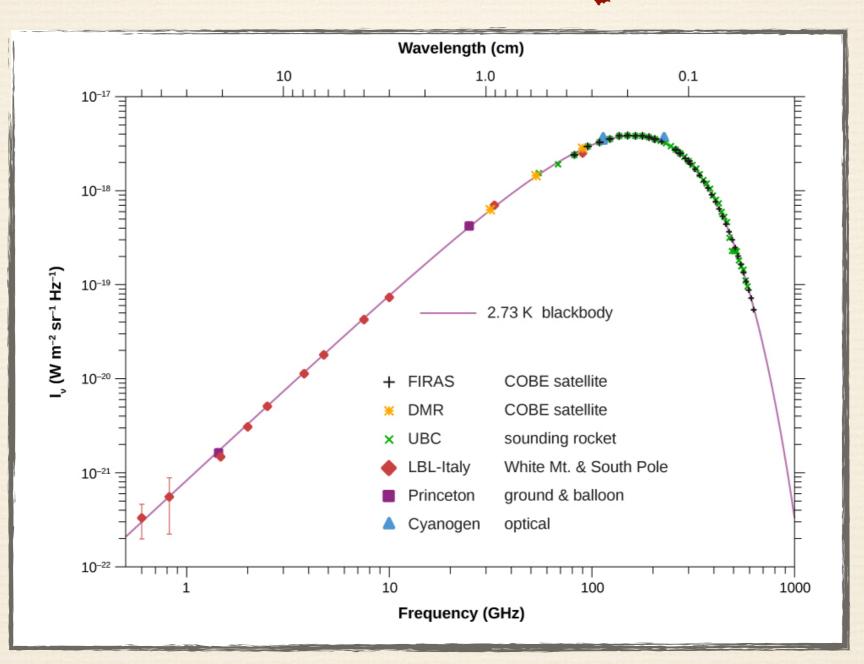


Robert Wilson

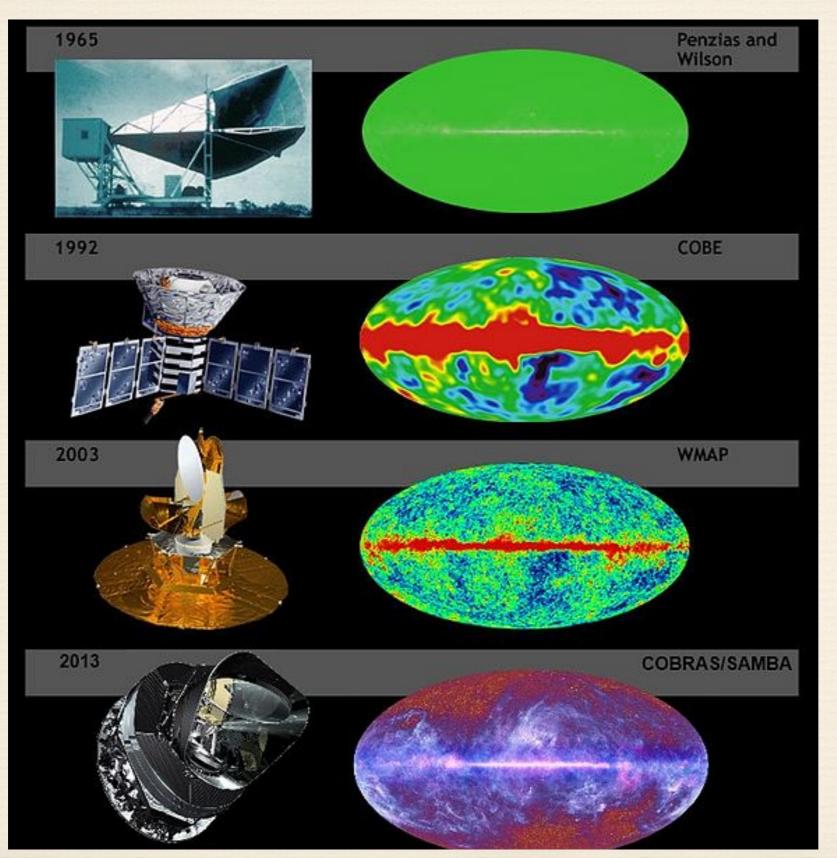


Arno Penzias

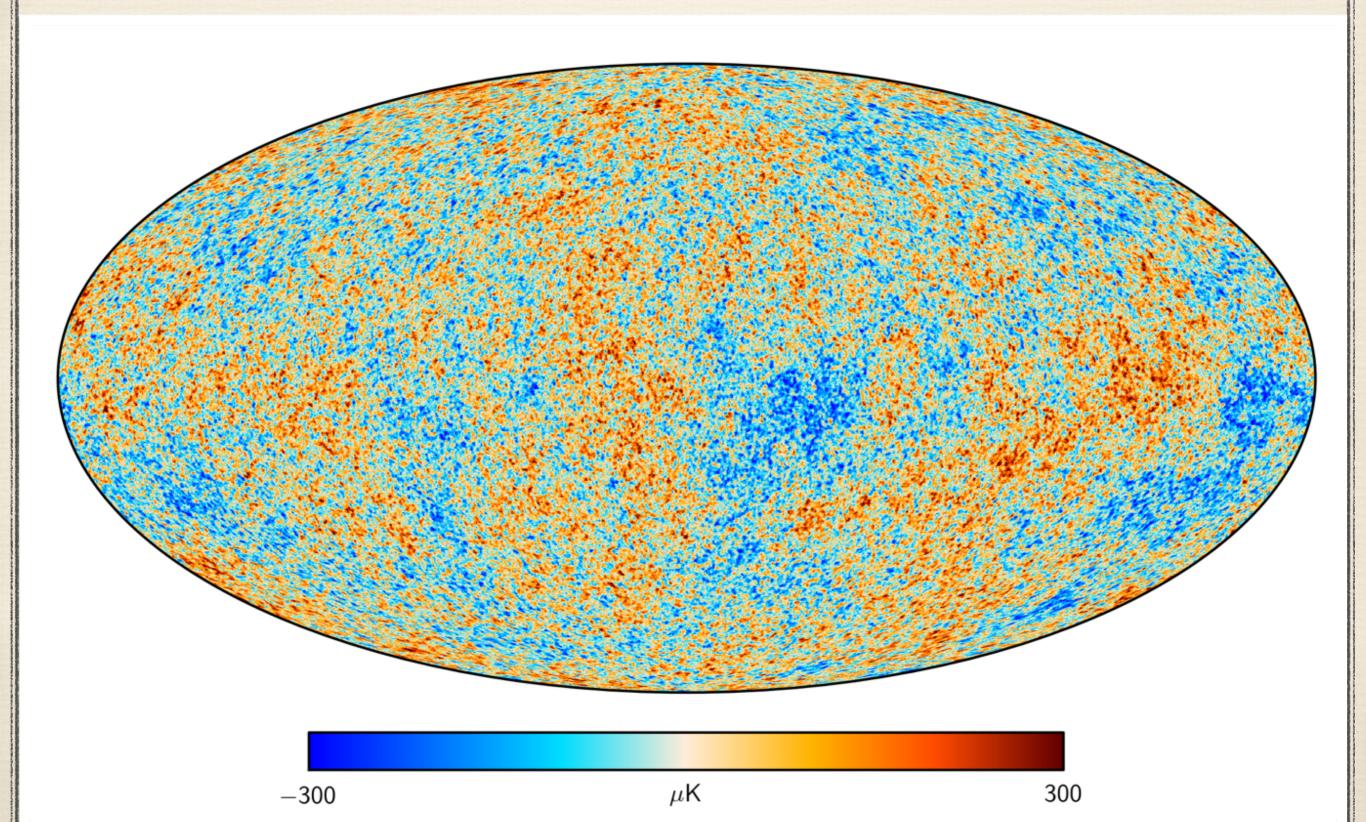
Spectrum of relic photons peaks at microwave frequencies



CMB temperature maps



Plancks mission



The cosmic microwave background is observed to be a 3K blackbody today, although in the past it must have been much hotter. We detect the peak of its emission today as microwaves. In the past, we would measure:

- A. Nothing, because the photons would not have reached us yet
- B. A much more energetic blackbody, peaking at shorter wavelengths
- C. A much more energetic blackbody, peaking at longer wavelengths
- D. A spectrum also in the microwave region, although it would not look like a blackbody
- E. A much fainter blackbody, peaking at longer wavelengths

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The Cosmological Principle

The cosmological principle is usually stated formally as

'Viewed on a sufficiently large scale, the properties of the Universe are the same for all observers.'

This amounts to the strongly philosophical statement that the part of the Universe which we can see is a fair sample, and that the same physical laws apply throughout. In essence, this in a sense says that the Universe is knowable and is playing fair with scientists

This is called the cosmological principle: the universe is homogeneous and isotropic

Recall that the Steady State Theory extends this to include time (universe invariant in time)

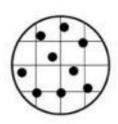
Is the Universe Static or Evolving?

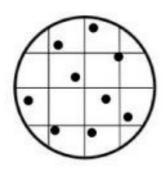
| Newton | 1600s | Static |
|---------------------------------|--|---|
| Einstein 1.0 | 1916 | Static ("greatest blunder") |
| Hubble | 1929 | Expanding |
| Einstein 2.0 (Lemaitre 1927) | 1929+ | Expanding |
| | Underlying spatial symmetry of the universe (isotropy: it looks the same in all directions, statistically) | |
| Bondi, Hoyle, Gold | 1948 Steady State Theory | Static |
| | Based on symmetry in time as well as space (more elegant) | |
| Gamov, Alpher, Herman | 1948 | Expanding |
| | Prediction of residual radiation from a hot initial universe | |
| Hoyle | 1950 | Coined "big bang" as a derogatory term |
| Refutation of SS Theory | 1960s-1970s | Discovery of cosmic background radiation, Galaxy evolution. |

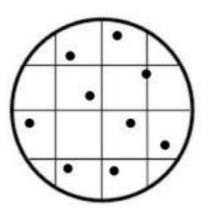
Big Bang Cosmology Matter dilates as the

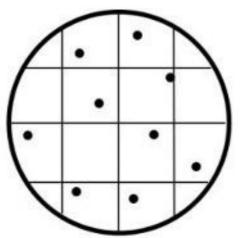
Universe expands

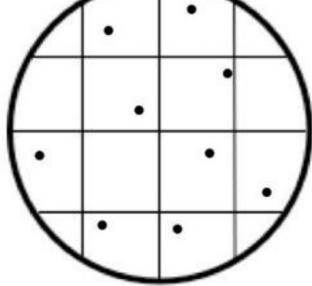








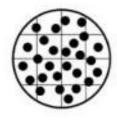


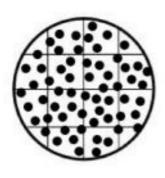


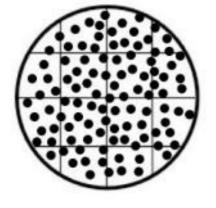
Steady-State Cosmology:

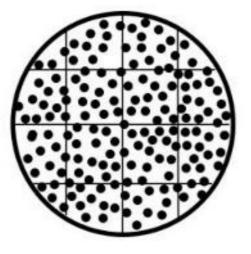
Matter is constantly created as the Universe expands

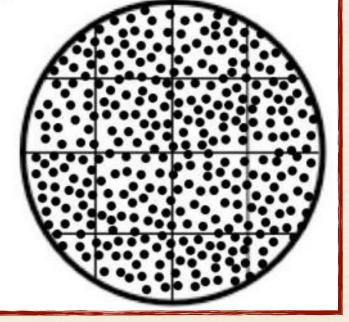












| "Big Bang" The First Three Minutes by Steven Weinberg | | | | | | | | |
|---|---------------------------|---------|---------------------|--|--|--|--|--|
| Time Temp Energy Density What's happening | | | | | | | | |
| .02 s | 10 ¹¹ K | 8.6 MeV | 4 x 10 ⁷ | The universe is mostly light. Electrons and positrons are created from light (pair-production) and destroyed at about equal rates. Protons and neutrons being changed back and forth, so about equal numbers. Only about one neutron or proton for each 10 9 photons. | | | | |
| .11 s | 10 3x10 K | 2.6 MeV | | Free neutrons decaying into protons, so there begins to be an excess of protons over neutrons. | | | | |
| 1.09 s | 10 ¹⁰ K | 860 keV | 4 x 10 ⁵ | Primeval fireball becomes transparent to neutrinos, so they are decoupled. It is still opaque to light and electromagnetic radiation of all wavelengths, so they are still contained. Electron-positron annihilation now proceeding faster than pair-production. | | | | |
| | | | | | | | | |
| 13.8 s | 3x10 K | 260 keV | | Below pair-production threshold. | | | | |
| 3 m 2 s | 10 ⁹ K | 86 keV | | Electrons and positrons nearly all gone. Photons and neutrinos are main constituents of the universe in terms of energy. Neutron decay leaves 86% protons, 14% neutrons but these represent a small fraction of the energy of the universe. | | | | |
| 3 m 46 s | 0.9x 10 ⁹ K | 78 keV | | Deuterium is now stable, so all the neutrons quickly combine to form deuterium and then helium. There is no more neutron decay since neutrons in nuclei are stable. Helium is about 26% by mass in the universe from this early time. Nothing heavier formed since there is no stable produce of mass 5. | | | | |
| 34 m 40 s | 3 x 10 ⁸ K | 26 keV | 10 | Deuterium is now stable, so all the neutrons quickly combine to form deuterium and then helium. There is no more neutron decay since neutrons in nuclei are stable. Helium is about 26% by mass in the universe from this early time. Nothing heavier formed since there is no stable produce of mass 5. | | | | |
| 7x 10 ⁵ yrs | 3000K | 0.26 eV | | Cool enough for hydrogen and helium nuclei to collect electrons and become stable atoms. Absence of ionized gas makes universe transparent to light for the first time. | | | | |
| 10 ¹⁰ yrs | 3 K | | | Living beings begin to analyze this process. | | | | |

STEVEN WEINBERG Winner of the 1979 Nobel Prize for Physics The First Three Minutes A Modern View of the Origin of the Universe WITH A MAJOR NEW AFTERWORD BY THE AUTHOR

nature

THE INTERNATIONAL WEEKLY JOURNAL OF SCIENCE

KILONOVA

Aftermath of the merger between two neutron stars PAGES 36, 64, 67, 71, 75,80 & 85

HEALTH

LESSONS FROM

Former funder seeks tech disruption for biomedicine PAGE 23 MOLECULAR ECOLOGY

EVOLUTION IN ACTION

Tracing mutations in 60,000 generations of bacteria
MGIS 42 & 45

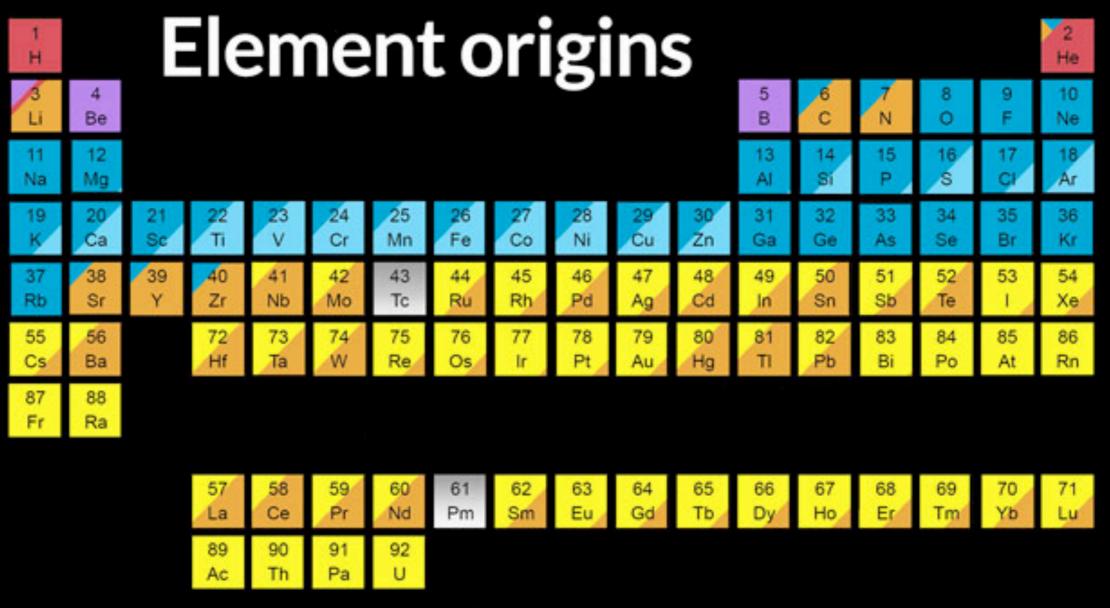
GENOMICS

CHROMOSOME COMPLEXITY

Two mechanisms that guide 3D structure of the genome MCIS 38 & 51 NATURE.COM/NATURE 2 November 2017 \$10

Vel 551, No. 767



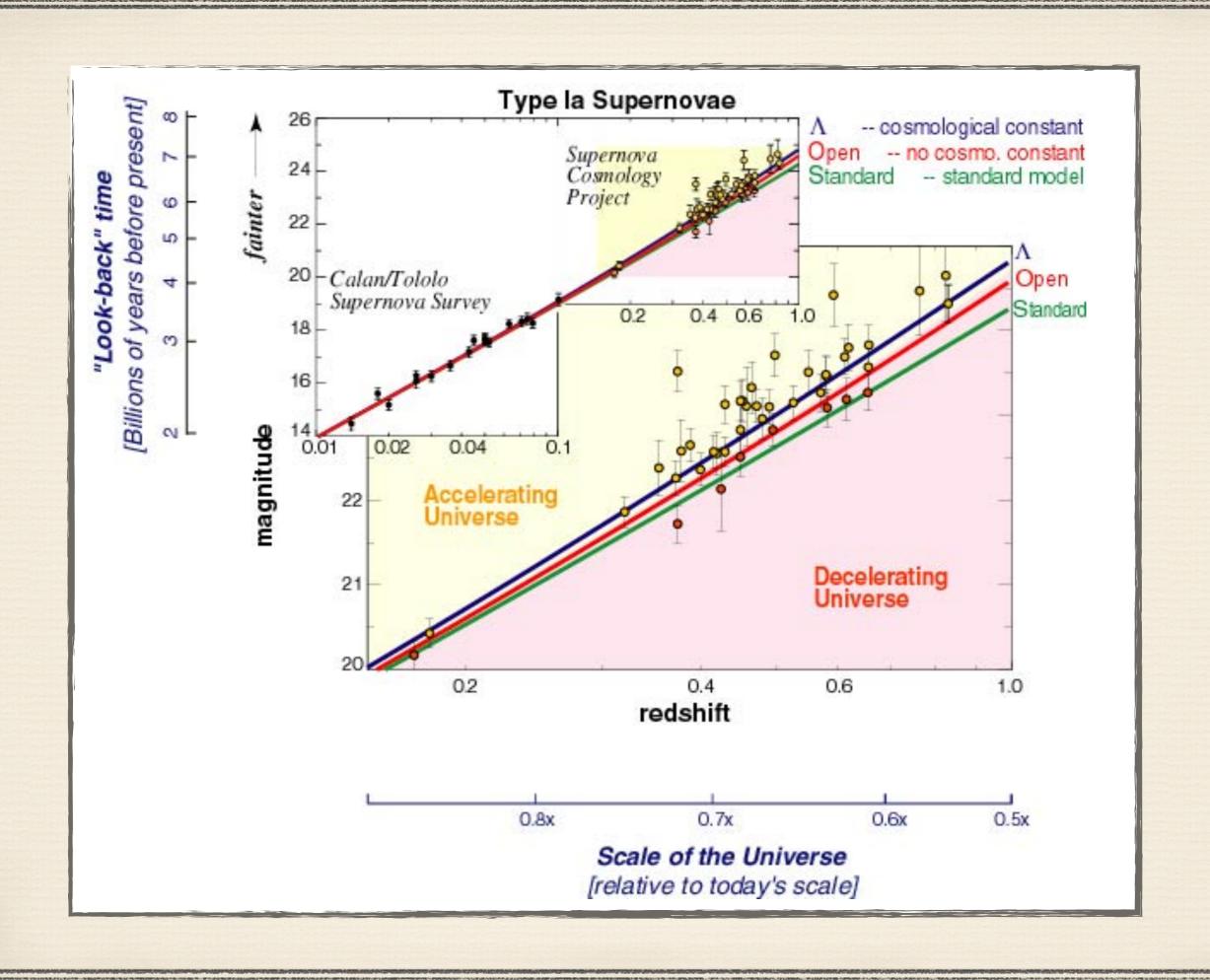


 The fireball from the Big Bang explosion is seen today as what?

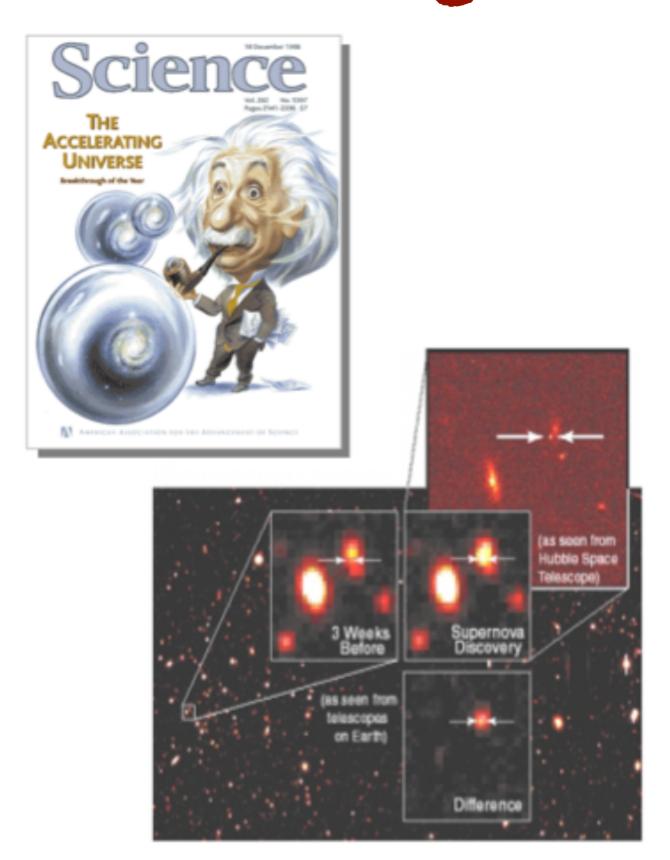
- A. Nuclear ash, mostly iron and silicon
- B. The cosmic microwave background
- C. Occasional outbreaks of supernovae
- D. A large Number of old stars
- E. Northern lights

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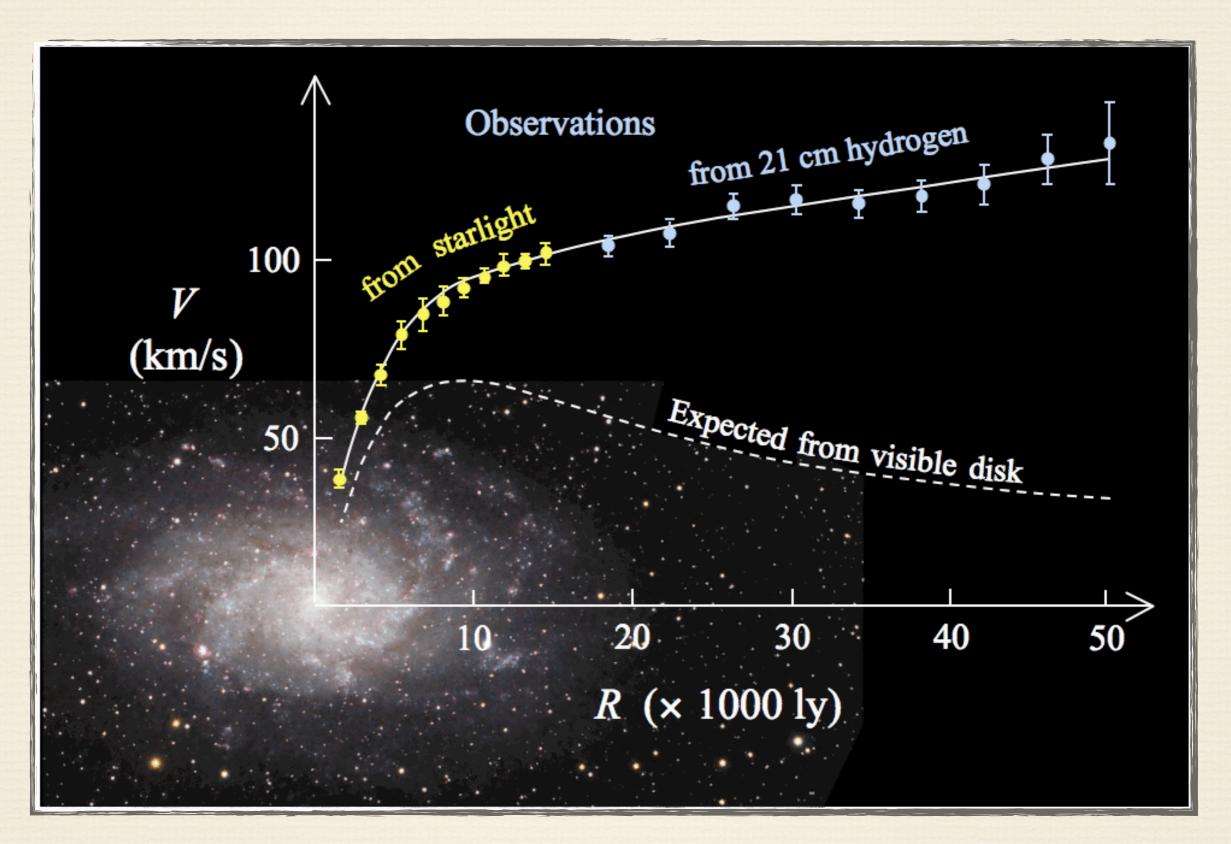
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Science's Breakthrough of the year: The accelerating Universe

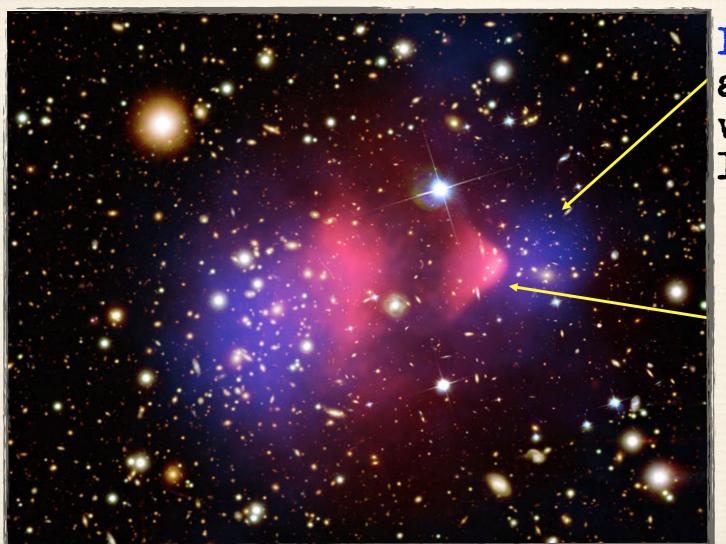


Rotation curve of M33



Dark Matter and X-Ray Gas in Cluster Mergers: The "Bullet Cluster" (1E 0657-56)

The dark matter clouds largely pass through each other, whereas the gas clouds collide and get shocked, and lag behind



Blue - dark matter, as inferred from weak gravitational lensing

Pink - X-ray gas

Recent observations of the very high-redshift Universe, using Supernovae Type Ia as standard candles, have revealed what ground-breaking discovery?

- A. Dark matter is actually completely made up of brown dwarfs and Black holes
- B. The Universe is not only expanding, but it is also accelerating
- C. A planet just like Earth, orbiting a star just like the Sun
- D. The Milky Way is actually at the center of the Universe
- E. The first wormhole which might allow human travel over vast distances

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- "Dark Matter" was first discovered through measurement of which of the following?
- A. Galaxy rotation curves
- B. Gravitational microlensing of compacto objects in the Milky Way halo
- C. The velocity of the Milky Way toward the Virgo cluster
- D. The velocity of stars deep within the Galactic center
- E. The velocity of Andromeda toward the Milky Way

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Cosmological Parameters

3. The dark energy density parameter

We can express a similar density parameter for lambda again by using the Friedmann equation and setting rh = 0

We then get

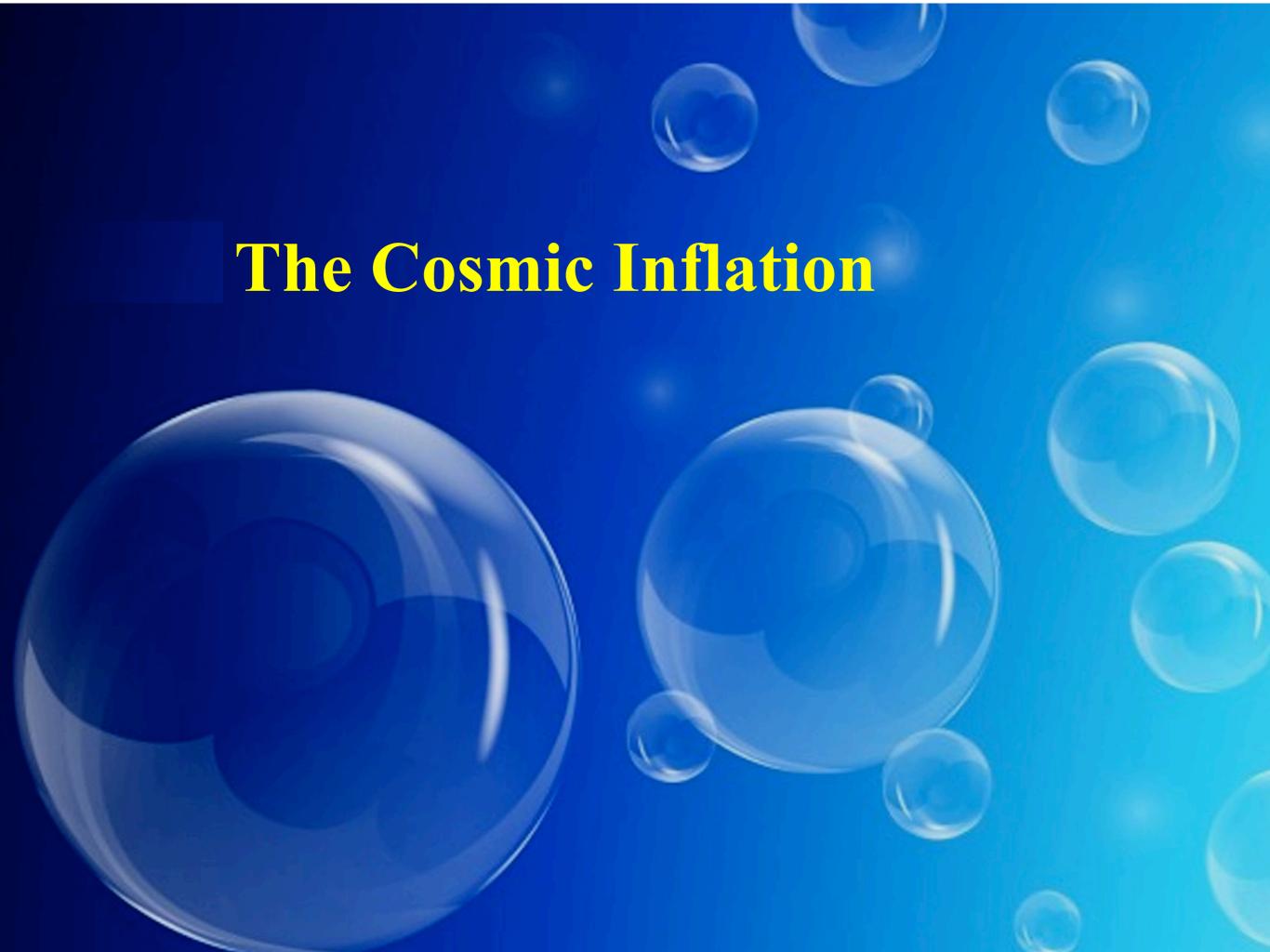
$$\Omega_{\Lambda}=rac{\Lambda c^2}{3H^2}^{
ho}$$

The total density parameter is then

$$\Omega = \Omega_M + \Omega_L$$

$$\Omega_L = \Omega_\Lambda = rac{
ho_\Lambda}{
ho_{
m crit}} rac{
ho_\Lambda}{
ho_{
m crit}}$$

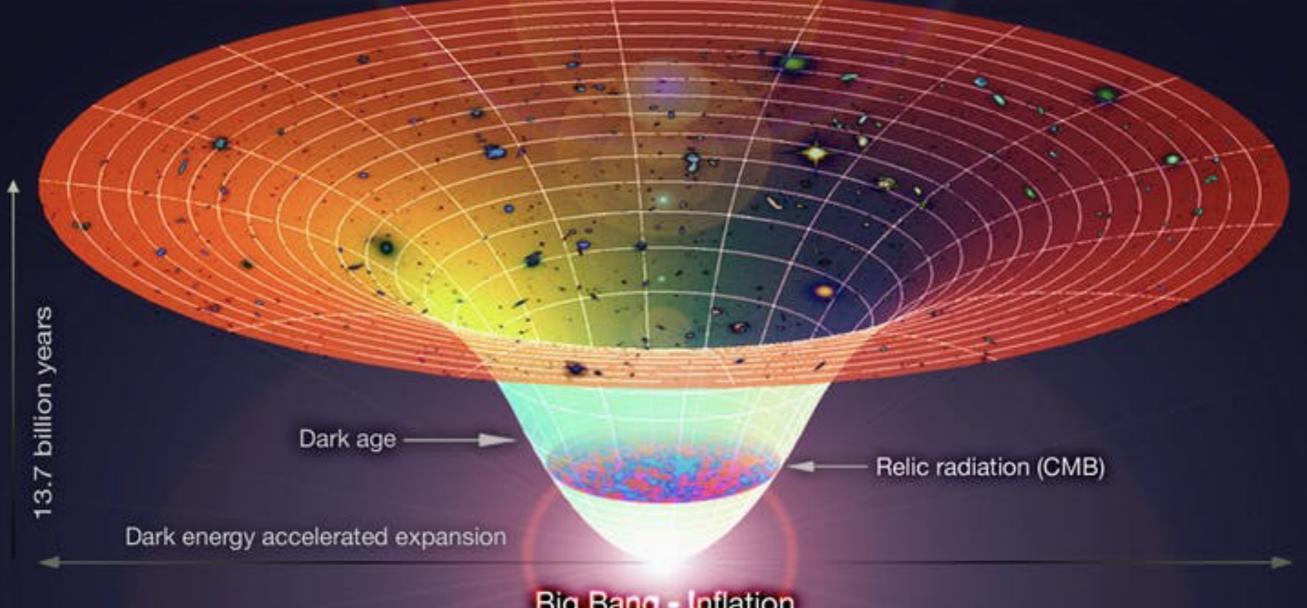
Cosmological model: ACDM?



Inflation

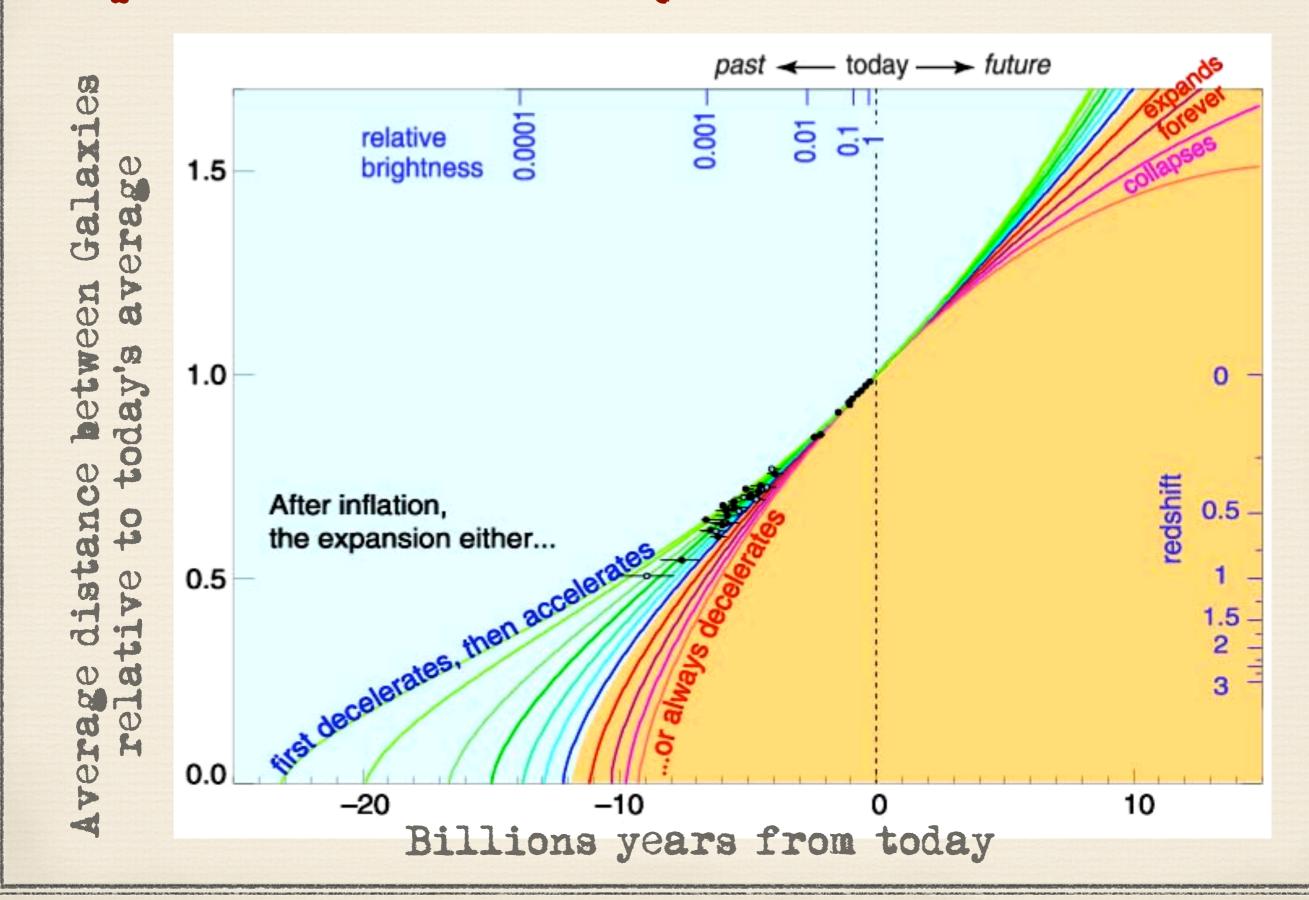
- * Physical models invoke a large reservoir of potential energy in the very early universe that decays to produce the sudden expansion
- * No consensus on the nature of the potential energy (scalar field with a slow-roll downhill or something else?)
- * The acceleration of the universe seen currently is a much milder version of inflation
- * An over-riding question is why now and why so little acceleration?

Accelerated Expansion of the Universe

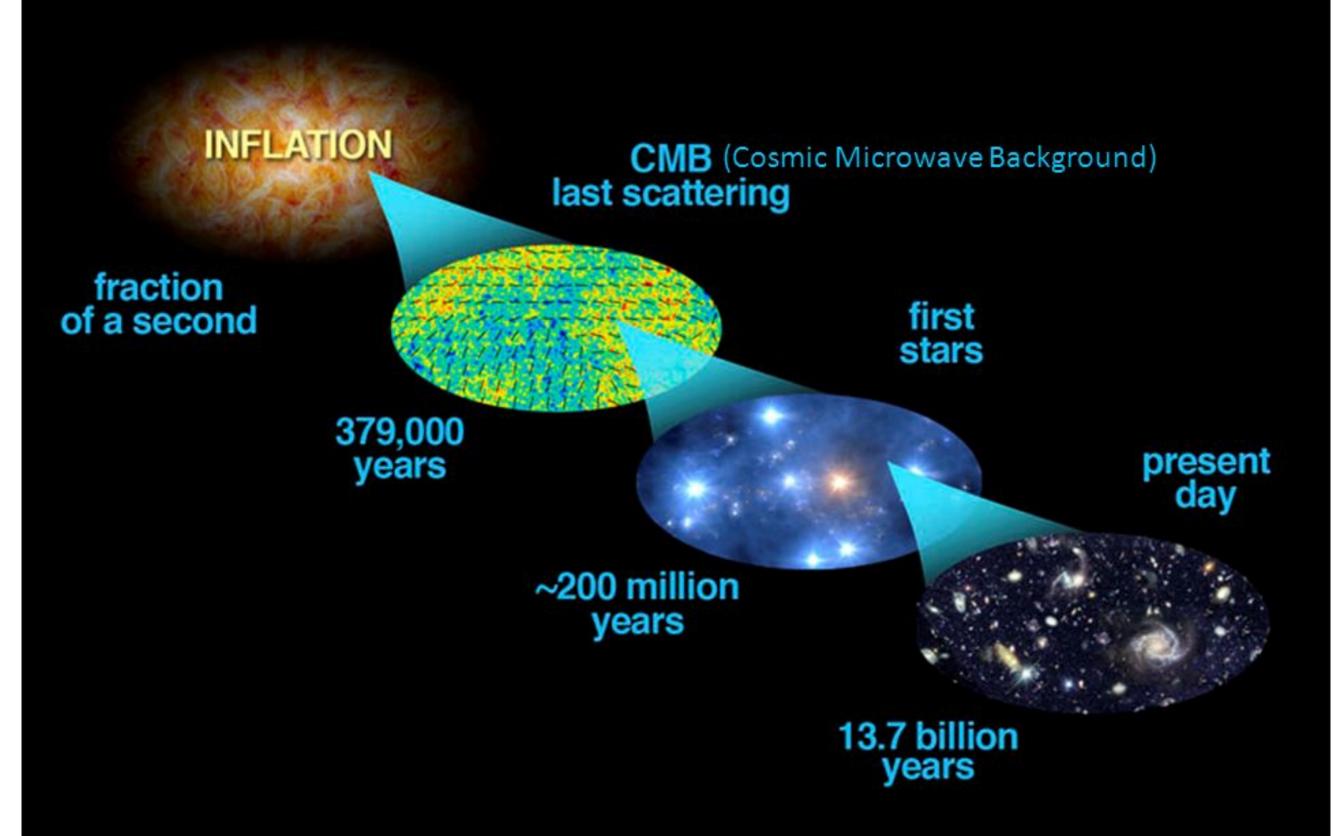


Big Bang - Inflation

Expansion History of the Universe



Brief History of time



Isotropy and Structure in the Universe Structure in the universe today:

Planets, stars, star clusters (globulars),

galaxies, galaxy clusters, superclusters

Why is the restructure and why does it have the size and massscales that we see?

Answer: primordial fluctuations + expansion + local gravity + ...

Primordial fluctuations:

Imposed in the big bang as a "scale-free" spectrum of spatial variations in energy

Inflation era: the universe expanded by a factor of 10^{60} in $< 10^{-30}$ sec

Expansion was at >> speedoflight

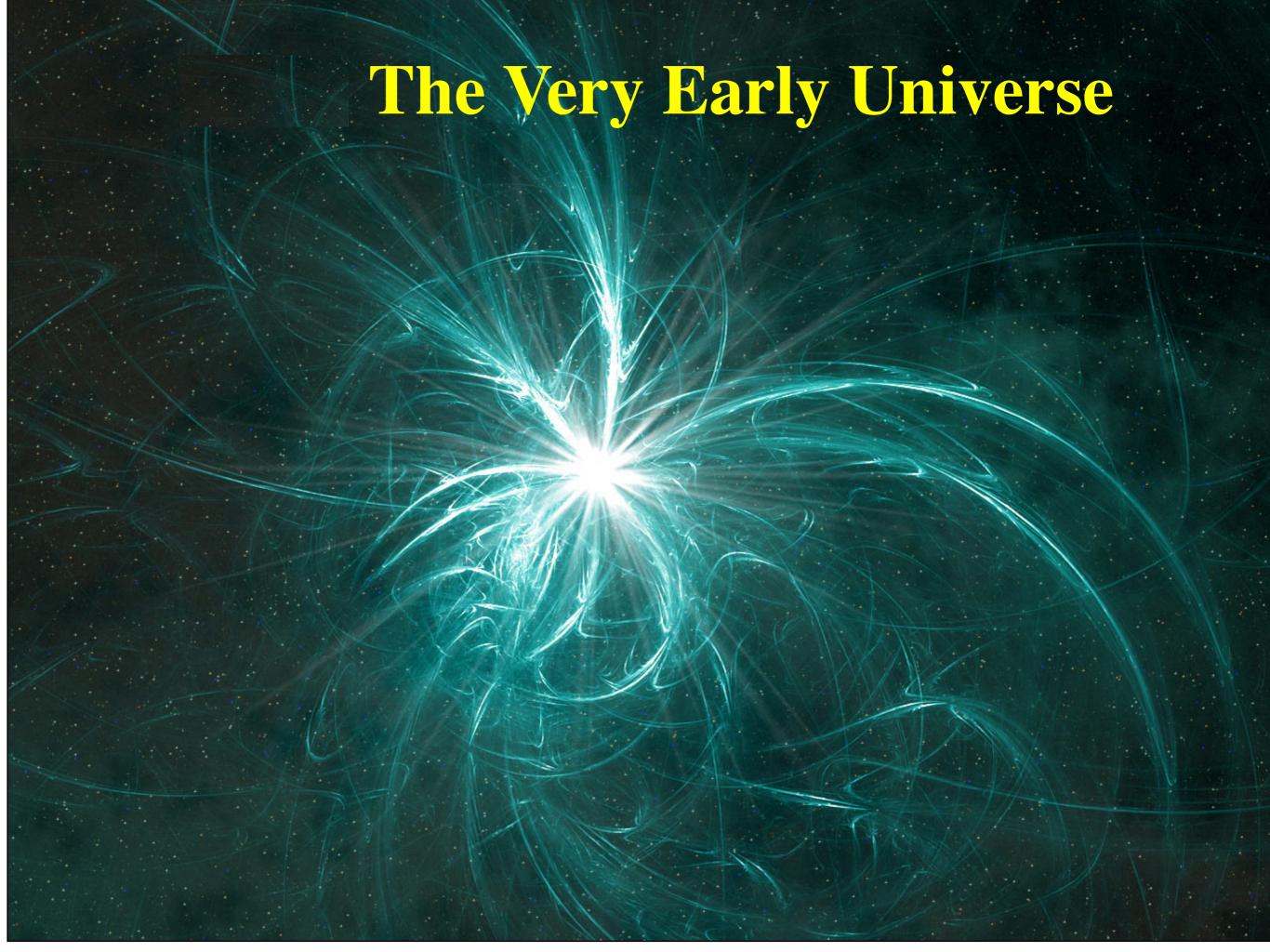
Why is this required observationally?

Two philosophical problems with the current Big Bang cosmology are that the Universe seems to be almst perfectly "flat" and that two parts of the Universe separated by more than the light travel time between them, seem to have identical properties (the "horizon" Problem) What suggested theory seems to naturally expalin these problems?

- A. Nothing so far
- B. Expansion
- C. Acceleration due to dark energy
- D. Inflation
- E. Grand Unified Theory

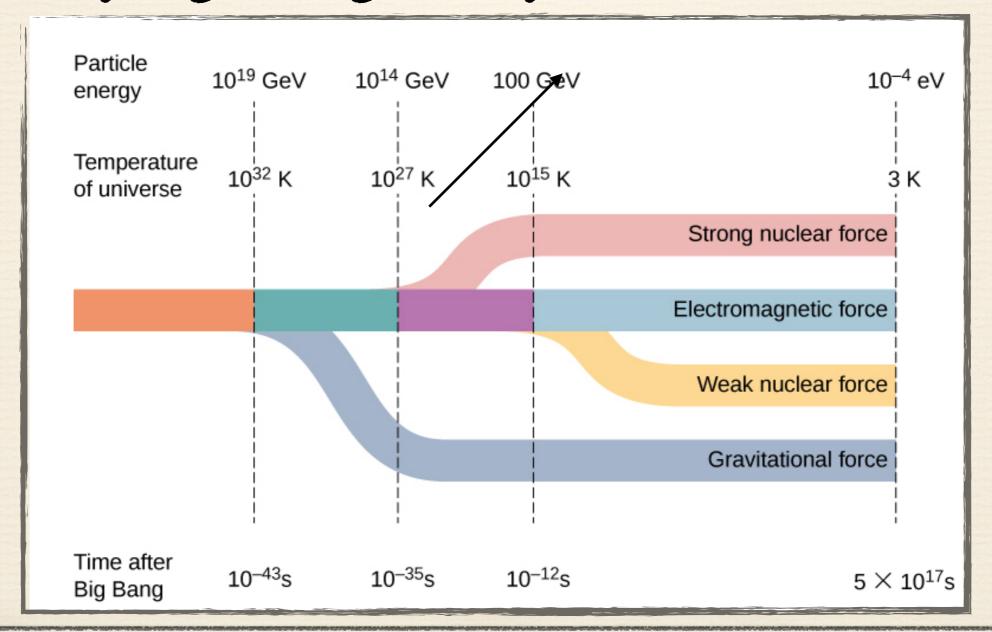
Two philosophical problems with the current Big Bang cosmology are that the Universe seems to be almst perfectly "flat" and that two parts of the Universe separated by more than the light travel time between them, seem to have identical properties (the "horizon" Problem) What suggested theory seems to naturally expalin these problems?

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Physical Interactions in the Early Universe

As we get closer to $t\to 0$ and $T\to \infty$, we probe physical regimes in which different fundamental interactions dominate. Their strength is a function of energy, and at sufficiently high energies they become unified



Planck Units

Proposed in 1899 by M. Planck, as the "natural" system of units based on the physical constants:

| Name | Dimension | Expression | Approx. SI equivalent measure |
|--------------------|---------------------|---|---------------------------------|
| Planck time | Time (T) | $t_P = \frac{l_P}{c} = \sqrt{\frac{\hbar G}{c^5}}$ | 5.39121 × 10 ⁻⁴⁴ s |
| Planck length | Length (L) | $l_P = \sqrt{\frac{\hbar G}{c^3}}$ | 1.61624 × 10 ⁻³⁵ m |
| Planck mass | Mass (M) | $m_P = \sqrt{\frac{\hbar c}{G}}$ | 2.17645 × 10 ⁻⁸ kg |
| Planck charge | Electric charge (Q) | $q_P = \sqrt{\hbar c 4\pi \epsilon_0}$ | 1.8755459 × 10 ⁻¹⁸ C |
| Planck temperature | Temperature (Θ) | $T_P = \frac{m_P c^2}{k} = \sqrt{\frac{\hbar c^5}{Gk^2}}$ | 1.41679 × 10 ³² K |

They may be indicative of the physical parameters and conditions at the era when gravity is unified with other forces ... assuming that G, c, and h do not change ... and that there are no other equally fundamental constants

Towards the Planck Era

"To Infinity, and Beyond..."

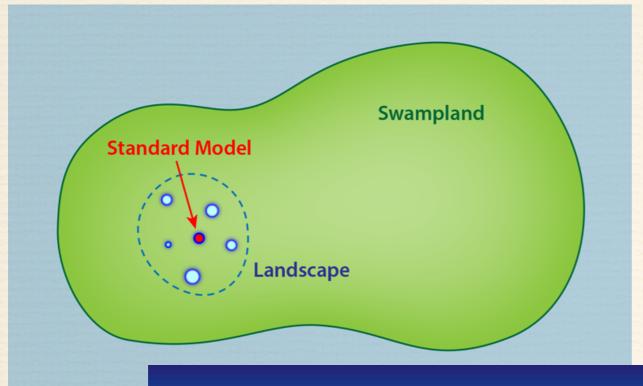


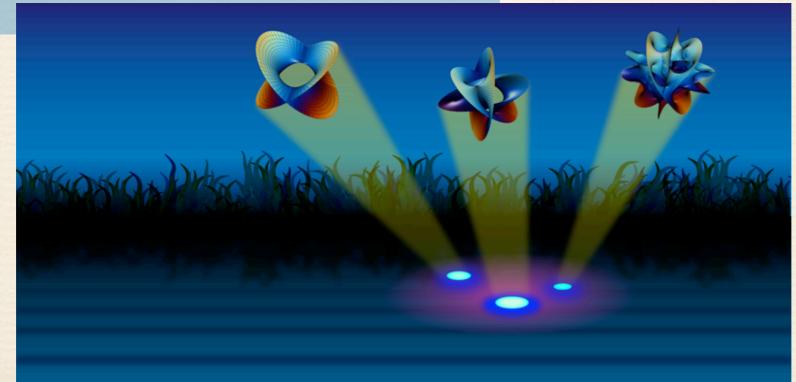
Probably gravity unified with the other forces

- so we need a theory of Quantum Gravity . Characteristic time ~ Planck Time ~ 10⁻⁴³ sec
 - . Characteristic time ~ Planck Time ~ 10⁻⁴⁹ sec after the Big Bang
- . Size of the universe then ~ Planck Length Highly Speculative theories include
- M-theory: particles are excitations on high
- dimensional
 membranes (D-branes). This includes...
- ** String Theory, where particles are different vibrations of one type of strings open string theory open string the string theory.
- * Ekpyrotic cosmology, String Landscape, ...

The future of fundamental physics?

String Theory prediction: all string models are incompatible with ACDM





Early in the Big Bang when temperatures are extremely high, particles can be created out of the radiation field. Which of the following statements about the creation of matter is FALSE?

- A. matter and energy are related, according to Einstein's E=mc²
- B. for unknown reasons, there happened to be slightly more matter than antimatter at the moment all the newly formed parciales "froze out"
- C. for every negatively charged electron formed, a positively charged neutrino was formed at the same time; the particle pair would then annihilate each other
- D. for every particle created there was also an antipatice created of the same mass
- E. as the temperature of the Universe dropped, the particle creation rate slowed

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The age of the universe (that is, the time since the Big Bang) is 14 billion years

The age of the Solar System is 4.56 billion years

Thus, the Solar System has existed for 32.6% of the age of the universe

For what percentage of the total age of the universe have existed: (i) helium nuclei, (ii) neutral atoms, (iii) galaxies, and (iv) the U.S.

Helium nuclei have been around since the time of primordial nucleosynthesis, at a time

 $t_{BBN} \approx 7 \text{ min} \approx 420 \text{ s}$

after the Big Bang

The age of the universe, expressed in seconds, is

$$t_{\rm U} = 1.4 \times 10^{10} \text{ yr} \left(\frac{3.16 \times 10^7 \text{ s}}{1 \text{ yr}} \right) = 4.4 \times 10^{17} \text{ s}$$

The fraction of the age of the universe during which helium nuclei have been around is

(There should be 13 nines after the decimal point I hope I counted them correctly!)

(ii) Neutral atoms have been around since the universe became transparent, at a time ttrans = 350,000 yr after the Big Bang

The fraction of the age of the universe during which neutral atoms have been around is

$$F = 1 - \frac{t_{\text{trans}}}{t_{\text{U}}} = 1 - \frac{3.5 \times 10^5 \text{ yr}}{1.4 \times 10^{10} \text{ yr}} = 1 - 0.000025 = 0.999975$$

Expressed as a percentage, this is 99.9975% of the age of the universe

(iii) Galaxies have been around since the universe had an age $tgal = 5 \times 10^8 yr$

The fraction of the age of the universe during which galaxies have been present is

$$F = 1 - \frac{t_{\text{gal}}}{t_{\text{U}}} = 1 - \frac{5 \times 10^8 \text{ yr}}{1.4 \times 10^{10} \text{ yr}} = 1 - 0.0357 = 0.964$$

Expressed as a percentage, this is 96.4% of the age of the universe

(iv) Dating from the Declaration of Independence, the U.S.A. has existed for 243 yr.

Written as a fraction of the age of the universe, the age of the U.S.A. is

$$F = \frac{243 \ yr}{1.4 \times 10^{10}} = 1.7 \times 10^{-8}$$

Expressed as a percentage, this is 0.0000017% of the age of the universe

Hydrogen has an absorption line at a wavelength λ_0 = 656.3 nm (as long as the hydrogen is at rest). You observe a distant galaxy for which the same hydrogen absorption line has a wavelength $\lambda = 715.4$ nm. (i) What is the redshift, $z = (\lambda - \lambda_0)/\lambda_0$, of the galaxy? (ii) What is the radial velocity of the galaxy, in kilometers per second? (iii) From Hubble's law, what is the distance to the galaxy? [Hint: assume $H_0 \approx 71 \text{ km/s/Mpc.}$]

QUERY 29 RONOMY 294Z: The History of the Universe (a) This first part is straight parbara Rydenug From the questablished Swetter on Robbis Ethin 4 Plugging these in to the formula provided find unit $3 \times 10^{-27} \, \mathrm{kg/m^{\circ}}$. If the matter consisted entirely of hydrogen many hydrogen $715.4 \, \mathrm{nm} - 656.3 \, \mathrm{nm}$ averages \overline{w} 009015 be contained in a cultural many hydrogen \overline{w} the universe? If the matter consisted entirely of regulation baseba Plyase on 15 kg aptece, how many vaseballs (on average) would be Redshift ostronomioakunited theimensionless number, meanling miasshoes single have convarints $m=1.7\times 10^{-27}\,\mathrm{kg}$. sthemasselewaiteteneths we bearted mithe eachenathyd

sthemasselevatveteneths we started mithe each enath adoption bittself voukebovald be digits in your ansewer here (0.09005)

However, rounding to 0.09 will have $= 1.76/m^3$ easier in the coming parts $7 \times 10^{-27} \, \mathrm{kg}$

1) [20 points] Today, the average densalph of an authorin the univers QUIERRY Son If the matter consisted entirely of hydrogen atom of hydrogen atom of hydrogen atom of hydrogen atom of hydrogen at the many hydrogen at the matter consisted entirely of hydrogen at the many hydrogen at the matter consisted entirely of hydrogen at the matter consisted entirely of hydrogen at the matter consisted entirely of hydrogen at the many hydroge (b) Usinge wours and the most eparts is and emixed radical dation do that la Can 2 Nepedal 15 y Sconings to be us new group to detail the remarkable wind the 3 × ima zukis astronomieteleunitateke conisested entirely of hydrogen atoms for average, would be contained in a the mass density to be a matter consisted entirely of regulation by the universe of the matter consisted entirely of regulation by per cubic meter would have to be As hip partifet kgrounded) this answery of a setters 4 (distiturage) wou Using z=0.09 instead, you would find -27 kg/m^3 $27 \text{ monomical would find } 27 \text{ the winderse} = 21.76 \text{ m}^3$.

The mass of a single hydrogen atom is $m=1.7 \times 10^{-27}$ which you can easily do without a calculator (since $9 \times 3 = 27$). (c) the mass density to be one as one pringle and chug opportunity. Hubble's law written $y = H_0$ d, relates the The mass of a single baseball is M = 0.145 kg. In order for density to be $\rho = 3 \times 60$ kg xm[0] the manner of baseballs per density to be $\rho = 3 \times 60$ kg xm[0] the manner of baseballs per density to be $\rho = 3 \times 60$ kg xm[0] the manner of baseballs per density to be $\rho = 3 \times 60$ kg xm[0] the manner of baseballs per density to be $\rho = 3 \times 60$ kg xm[0] the manner of baseballs per density to be $\rho = 3 \times 60$ kg xm[0] the manner of baseballs per density to be $\rho = 3 \times 60$ kg xm[0] the manner of baseballs per density to be $\rho = 3 \times 60$ kg xm[0] the manner of baseballs per density to be $\rho = 3 \times 60$ kg xm[0] the manner of baseballs per density to be $\rho = 3 \times 60$ kg xm[0] the manner of baseballs per density to be $\rho = 3 \times 60$ kg xm[0] the manner of baseballs per density to be $\rho = 3 \times 60$ kg xm[0] the manner of baseballs per density to be $\rho = 3 \times 60$ kg xm[0] the manner of baseballs per density to be $\rho = 3 \times 60$ kg xm[0] the manner of baseballs per density to be $\rho = 3 \times 60$ kg xm[0] the manner of baseballs per density the baseballs per density to be $\rho = 3 \times 60$ kg xm[0] the manner of baseballs per density the baseballs per density the baseballs per density the baseballs per density the baseball Using Hould hake (8/Mpc and the answer from part (h)7(1/find:

The mass of a single hydrogen atom is $m = 1.7 \times 10^{-3}$ Chemistry to be $\rho = 3 \times 10^{-27} \,\mathrm{kg/m^3}$, the number of It well so be textremely agateful with units to avoid mistakes, particularly with velocities! To be sure to get this correct, I rewrite my 76/mits as conventional fractions $\frac{n}{n} = \frac{1.7 \times 10^{-27} \, \text{kg}}{1.7 \times 10^{-27} \, \text{kg}}$ The Hubbilla Constant mil, km/s/Npce, thus checomastel of Spaces. Mpc Plugwidensthis back in, I have: The mass of a single baseball is $M = 0.145 \,\mathrm{kg}$. In or density to be $\frac{v}{H}\rho = \frac{27.95}{27.95} \times 10^{-27/9c} \text{ graph } \frac{27.915}{71 \text{ large}} \text{ graph } \frac{27.915}{11.100} \text{ where } \frac{39.50 \text{ min}}{100} \text{ has ebase } \frac{1}{100} = \frac{1}{100} \times 10^{-100} \text{ min} = \frac{1}{100}$ Please notice that the km and s units cancel completely, leaving behind Mpc (1.5 × 1011 m)3 It's always important to check whether or not the units make sense. Fortunately, Mpc is a measure of distance, which is what we're looking for

As we have seen in the lectures, if the Hubble constant is $H_0 = 71$ km/s/Mpc, then the Hubble time is $1/H_0 = 14$ billionyears. Sir Edwin Hubble himself, because he grossly underestimated the distance to galaxies, believed that the Hubble constant was $H_0 = 500$ km/s/Mpc.

For $H_0 = 500 \text{ km/s/Mpc}$, what is $1/H_0$, in billions of years?

You can either calculate the new Hubble time directly with unit conversion, or you can solve for it by comparison to the actual Hubble time using ratios. Both methods give the same answer (i.e., they both work) pines y The temperature of the connic books ered dight to devis f, take great t the time the universe became transparent, the temperature of the care to make sure that you cancel out your units background light was $T \approx 3000\,\mathrm{K}$. This means that the universe has ed by appearing of 1000 since it became transparent. If the density of today in 2thexpressions aquestions I deliberent in a 3K. At the time the universe became transparent, the temperature of the vemotecomandary of the form from the associate mistakes: sider a cubapathat bisa exclaration of since it were transporant all the plansion of verse. The edges of the Epc 12 10-27 kg/m³ what was the length matter when mow lume of the curverse became transparent? They became transparent? They was the length matter when mow lume of the curverse became transparent? They was the length matter when mow lume of the curverse became transparent? The mithself keepstine the atherwise plant here at length $\ell_{\rm polest}$ by the converge of the cube remains constant as the universe expands. At $M=\rho_{\rm now}\ell_{\rm now}^3=3\times 10^{-2}$ kg. Since matter is not created or destroyed, e thefuniters M inside the cube remains constant as the universe expands. At the tilength of the universe beganne transparent, the expanding cube had sides of $\times 10^{-17}$. In length of 10^6 pc 10^6 length

 $(3)(\mathbf{9})$

nside Parciulse Whaterise extra and the calonic background light tedal expansion of The time the universe became transparent the temperature of the 0 mover 0 mic background high was $T \approx 3000 \, \text{K}$. This means that the universe has column of the 0 mass it contains is expanded by a factor of loos $s = 1 \, \text{m}$ and thus the $l = 1 \, \text{m}$ is $l = 1 \, \text{m}$. pnowdiffer to tay 3 is \$\square\$ 10\frac{3}{\times} \text{log} 27 \kg/mce unatter is not signest advarudes troyed, assPleasochdotectwoothingsnsfinstlyhe nearly ealand Athe units ne can dely each backen have along with the general expansion of december of the currently have a length converge of the edges of the currently have a length converge of the edges of the currently have a length converge of the edges of the currently have a length converge of the edges of the currently have a length converge of the edges of the currently have a length converge of the edges of the currently have a length converge of the edges of the currently have a length converge of the edges of the edges of the currently have a length converge of the edges of the edges of the currently have a length converge of the edges The color description of the probability of the passe of t the ensite incheraises became teansparent the manding webshad fides was $rans_{The} = \frac{M}{\text{Mansity within.}} = \frac{3 \times 10^{-27} \text{ kg}}{\text{Mansity within.}} = \frac{3 \times 10^{-27} \text{ kg}}{1.62 \times 10^{-27} \text{ kg}} = \frac{3 \times 10^{-27} \text{ kg}}{1.62 \times 10^{-27} \text{ kg}} = \frac{3 \times 10^{-27} \text{ kg}}{1.62 \times 10^{-27} \text{ kg}} = \frac{3 \times 10^{-27} \text{ kg}}{1.62 \times 10^{-27} \text{ kg}} = \frac{3 \times 10^{-27} \text{ kg}}{1.62 \times 10^{-27} \text{ kg}} = \frac{3 \times 10^{-27} \text{ kg}}{1.62 \times 10^{-27} \text{ kg}} = \frac{3 \times 10^{-27} \text{ kg}}{1.62 \times 10^{-27} \text{ kg}} = \frac{3 \times 10^{-27} \text{ kg}}{1.62 \times 10^{-27} \text{ kg}} = \frac{3 \times 10^{-27} \text{ kg}}{1.62 \times 10^{-27} \text{ kg}} = \frac{3 \times 10^{-27} \text{ kg}}{1.62 \times 10^{-27} \text{ kg}} = \frac{3 \times 10^{-27} \text{ kg}}{1.62 \times 10^{-27} \text{ kg}} = \frac{3 \times 10^{-27} \text{ kg}}{1.62 \times 10^{-27} \text{ kg}} = \frac{3 \times 10^{-27} \text{ kg}}{1.62 \times 10^{-27} \text{ kg}} = \frac{3 \times 10^{-27} \text{ kg}}{1.62 \times 10^{-27} \text{ kg}} = \frac{3 \times 10^{-27} \text{ kg}}{1.62 \times 10^{-27} \text{ kg}} = \frac{3 \times 10^{-27} \text{ kg}}{1.62 \times 10^{-27} \text{ kg}} = \frac{3 \times 10^{-27} \text{ kg}}{1.62 \times 10^{-27} \text{ kg}} = \frac{3 \times 10^{-27} \text{ kg}}{1.62 \times 10^{-27} \text{ kg}} = \frac{3 \times 10^{-27} \text{ kg}}{1.62 \times 10^{-27} \text{ kg}} = \frac{3 \times 10^{-27} \text{ kg}}{1.62 \times 10^{-27} \text{ kg}} = \frac{3 \times 10^{-27} \text{ kg}}{1.62 \times 10^{-27} \text{ kg}} = \frac{3 \times 10^{-27} \text{ kg}}{1.62 \times 10^{-27} \text{ kg}} = \frac{3 \times 10^{-27} \text{ kg}}{1.62 \times 10^{-27} \text{ kg}} = \frac{3 \times 10^{-27} \text{ kg}}{1.62 \times 10^{-27} \text{ kg}} = \frac{3 \times 10^{-27} \text{ kg}}{1.62 \times 10^{-27} \text{ kg}} = \frac{3 \times 10^{-27} \text{ kg}}{1.62 \times 10^{-27} \text{ kg}} = \frac{3 \times 10^{-27} \text{ kg}}{1.62 \times 10^{-27} \text{ kg}} = \frac{3 \times 10^{-27} \text{ kg}}{1.62 \times 10^{-27} \text{ kg}} = \frac{3 \times 10^{-27} \text{ kg}}{1.62 \times 10^{-27} \text{ kg}} = \frac{3 \times 10^{-27} \text{ kg}}{1.62 \times 10^{-27} \text{ kg}} = \frac{3 \times 10^{-27} \text{ kg}}{1.62 \times 10^{-27} \text{ kg}} = \frac{3 \times 10^{-27} \text{ kg}}{1.62 \times 10^{-27} \text{ kg}} = \frac{3 \times 10^{-27} \text{ kg}}{1.62 \times 10^{-27} \text{ kg}} = \frac{3 \times 10^{-27} \text{ kg}}{1.62 \times 10^{-27} \text{ kg}} = \frac{3 \times 10^{-27} \text{ kg}}{1.62 \times 10^{-27} \text{ kg}} = \frac{3 \times 10^{-27} \text{ kg}}{1.62 \times 10^{-27} \text{ kg}} = \frac{3 \times 10^{-27} \text{ kg}}{1.62 \times 10^{-27} \text{ kg}} = \frac{3 \times 10^{-27} \text{ kg}}{1.62 \times 10^{-27} \text{ kg}} = \frac{3 \times 10^{-27} \text{ kg}}{1.62 \times 10^{-27} \text{ kg}} = \frac{3 \times 10^{-27} \text{ kg}}{1.62 \times 10^{-27} \text{ kg}} =$ gths in the universe increase by a factor of some theorem and, (then the of onvertime astheyabove realine bito years, I get: If lengths in the universe increase by a factor of one thousand, then the density of matter decreases by a factor of one billion. $\frac{1}{H_0} = (6.173 \times 10^{16} \text{ s}) \left(\frac{1 \text{ yr}}{3.15 \times 10^7 \text{ s}}\right) = \frac{6.173 \times 10^{16}}{3.15 \times 10^7} \text{ yr} = 1.96 \times 10^9 \text{ yr} = 1.96 \text{ billion years}$

$$t_{\rm trans} = \frac{\ell_{\rm now}}{1000} = \frac{1 \,\mathrm{m}}{1000} = 0.001 \,\mathrm{m} \ .$$
 (3)

The density within the box when the universe became transparent was

 $\rho_{\rm trans} = \frac{M}{\sqrt{3}} = \frac{3 \times 10^{-27} \, {\rm kg}}{(0.001 \, {\rm m})^3} = \frac{3 \times 10^{-27} \, {\rm kg}}{10001 \, {\rm m}^3} = 3 \times 10^{-18} \, {\rm kg/m^3} \, . \qquad (4)$ Alternatively, $\frac{1}{\sqrt{9}} = \frac{3 \times 10^{-27} \, {\rm kg}}{10001 \, {\rm m}^3} = 3 \times 10^{-18} \, {\rm kg/m^3} \, . \qquad (4)$ The new 1/H₀ must be smaller than the priverse increase by a factor of one thousand, then the ratio of H₀ values (if H₀ gets bigger, then 1/H₀ must get smaller) Doing this you would find

$$\frac{1}{H_0} = \left(\frac{71 \text{ km/s/Mpc}}{500 \text{ km/s/Mpc}}\right) \cdot 14 \text{ billion years} = 0.142 \cdot 14 \text{ billion years} = 1.99 \text{ billion years}$$

Note that all the units in the H₀ ratio above cancelled elimined that ely. Setting up the problem to intentionally cancel units is a useful way to avoid needless conversion mistakes

There are 411,000,000 cosmic microwave photons per cubic meter of the universe. The average energy of a cosmic microwave photon is very small: only $E = 1.02 \times 10^{-22}$ joules. What is the energy density of the Cosmic Microwave Background, in joules per cubic meter? Using Einstein's relation, E = mc2, what is the equivalent mass density, in kilograms per cubic meter? What fraction of the critical density, perit = 10-26 kg/m3, does this density represent?

First, compute the energy density of the CMB. We know the number of photons per unit volume 20 points 10 thous time and the standardinal of thetreich carekground light washolon 4.8 Figure 1 the time of primardial nucleosynthesis, the tement of the the the tement of the the tement of the temperature of te the time experimental of primardial nucleosynthesis was 1. heotemperaturat the time Johnson by a factor of The tempe of the the thought of the party Tnusing E3-Kmc2

a factor of a since the time of primordial nucleosynthesis. That is, a cube that

tianneonarping rediceling utche correct heavisers Toh atteis as c of length $t_{\text{now}} = 1 \text{ m had sides of length}$ When using the relation E = mc2, take care with your units!! Since 1 Joule = $1 \text{ kg/m}^2 / \text{s}^2$, you Must the c = $3.0 \text{ x} 10^8 \text{ m/s!!}$ $= 6.25 \times 10^{-10}$ If you have E in Govleson in kg/6 but use c = $3.0 \text{ x} 10^8 \text{ m/s!}$ the units DO NOT WORK as expected, because km/s does not properly cancel the m/s built into Joules This is a very ne argument as in the previous problem, we dedu t the time of primordial nucleosynthesis was

